Introduction

The study described in this report constitutes part of an ongoing research project in the area of task planning under uncertainty. Traditional approaches to task planning assume that the planner has access to all of the world information needed to develop a complete, correct plan which can then be executed in its entirety by an agent. Of course, for most complex domains, having all of the necessary world information at plan time cannot be assumed. We have implemented a planner, BUMP, which is capable of interleaving planning and execution. BUMP is able to defer portions of the planning process which depend on unknown or uncertain information until the information in question can be obtained through sensors. In this case, BUMP inserts sensor operations directly into the plan which the agent executes to enable further planning.

Alternately, BUMP may choose to assume a default value for the uncertain information rather than plan to sense it. We call this distinction the defer/default question, and it has played a central role in guiding our recent research efforts.

Deferral and defaulting each have strengths and weaknesses. Deferral can be attractive with good sensors because it reduces planner uncertainty, however, sensing can become prohibitively expensive. In addition, satisfying preconditions for sensor operations can in itself be time-consuming, and as we will see, increases the probability of performing premature actions.

Defaulting can be risky, but it allows the planner to complete more of the plan before execution begins. This allows the planner to see further into the plan and detect problems which may lie beyond the horizon of the deferral point. As domain uncertainty increases however, further planning becomes increasingly arbitrary.

In general, it is difficult to know whether to defer and sense a given uncertain value or simply choose a default value and face the risks. Deciding on the best strategy for a given planning problem consists of computing the tradeoffs of various strategies, but as we will see, such a computation quickly becomes intractable for even a modest degree of uncertainty, suggesting the need for heuristic techniques.

Purpose of Study

The experiments described here were designed to answer general questions about factors that influence the plan quality, and how to use those factors when deciding on planning strategies. In this section we discuss three types of planning strategies and three measures of plan quality. It is useful to think of the quality measures as functions to minimize or maximize, and the strategies as means to that end.

Planning Factors

We have identified the following as important factors of task planning with sensors. Our studies have shown that by intelligently controlling these factors, a planner can improve its performance, often dramatically. Thus, we define an overall planning strategy as a set of algorithms to determine each of the following parameters for a given problem instance.

Goal ordering: We found it advantageous to carefully order the planner’s initial goals based on the amount and type of unknown information at the start of planning. Thus, we varied and examined goal orders to determine heuristics for a goal ordering strategy.

When to sense: A critical decision when interleaving planning and execution is when to switch from one to the other. In related research, [Olawsky and Gini, 1990] identified two general strategies to manage the transfer of control between the planning and execution modules (i.e., control strategies). In each stra-
egy, if the planner discovers that it requires unknown information it inserts a sensor operation into the plan to obtain the information. It then plans to satisfy any preconditions of this sensor operation.

In the first strategy, known as Stop and Execute (SE), when the planner encounters a goal whose achievement depends on information it has planned to sense, control is transferred to the execution module. The sensor process and all processes ordered before it in the current partial plan are executed. Control then returns to the planner.

In the second strategy, Continue Elsewhere (CE), goals whose achievement depends on information to be sensed are deferred. Planning continues elsewhere. Only when all goals are either planned to completion or deferred does execution initially commence. Execution halts after each sensor operation to allow completion of a deferred goal. In general, CE allows much more planning, albeit less informed planning, to occur ahead of the first execution phase.

We believe these two strategies to be of particular interest because they seem to be the only truly domain independent control strategies which we have found useful. Any other strategies we have considered are not general-purpose, and are only useful under rather specific circumstances.

What to sense: Finally, there is the question of which uncertain quantities to sense and which to default. We will refer to this as the deferral strategy. Choosing a reasonable deferral strategy requires careful consideration of domain-specific factors such as default reliabilities, sensor reliabilities, planning costs, execution costs, and the cost of human intervention.

Plan Quality Criteria
Before discussing the strategies above, we must be clear as to the objectives they are intended to serve. We call these objectives plan quality criteria, and we have identified and gathered data on a number of them, each of which could stand alone, or be used in conjunction with other criteria as a measure of plan quality.

Success Rates: For this measure of planner performance, we computed the percentage of problems in which BUMP was able to construct plans in which no processes needed to be undone as a result of being executed prematurely. One of the major difficulties in interleaving planning and execution is to keep the robot from performing actions which may interfere with goals not yet considered. The most common example of this in our experiments occurred when the robot bolted closed a tool box only to discover that it contained a wrench (or bolt) needed to accomplish a later goal. Under this criterion we considered such plans failures, in effect assuming the agent was unable to recover from such premature action.

Execution Cost: For this criterion we measured the cost of all actions to be performed in the final plan when the planner is allowed to recover from premature action (i.e. undo and redo these actions). This provided us with some indication of how inefficient the inferior solutions were to previously unsuccessful problems. For these experiments, we simply counted each instantiated process (action) in the plan as having unit cost, although it would be trivial to assign varying costs to various types of actions.

Planning Cost: Finally, in some experiments we tracked the amount of planning work done by the planner. Since BUMP is an agenda-based planner, a reasonably accurate indication of planning work is the number of items it placed on its agenda.

Experiments in the Tool Box World
Each experiment consisted of running BUMP on a carefully controlled set of problems. We selected the most challenging subset of problems and measured BUMP’s performance in solving each of them.

All of the experiments consisted of problems in the tool box world. In this world, the robot is in a room with n tool boxes, each containing wrenches and bolts of various sizes. The robot knows the initial locations of the wrenches and bolts. Bolts are identified by a unique name, and wrenches are identified by size. The robot has been instructed to close and bolt one or more tool boxes with particular bolts. To perform each bolting operation, the robot must use a wrench of a size that matches the bolt. A sensor is available that can classify bolts by their size (e.g., a number from 1 to 10). For simplicity, the bolt sizes are indicated along the same scale as the wrench sizes. We also assume the robot has a tool belt into which it can put an unlimited number of bolts and wrenches.¹

¹We are not concerned here with the arm-empty conditions as used in typical definitions of the blocks world. Our main goal in defining this domain is to study how sensor use can be interleaved with planning.
In effect, this tests the planner on the hardest problems, i.e., those most likely to involve premature action.

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Table 1: Summary of experiments for success rates, execution cost, and planning cost criteria.

<table>
<thead>
<tr>
<th>Exp</th>
<th>Boxes</th>
<th>Quality</th>
<th>Control Strategy</th>
<th>Goal Orders</th>
<th>Num of Unknowns</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3</td>
<td>success</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>success</td>
<td>CE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>e-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>4</td>
<td>3</td>
<td>e-cost</td>
<td>CE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td>p-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>6</td>
<td>3</td>
<td>p-cost</td>
<td>CE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>7</td>
<td>4</td>
<td>e-cost</td>
<td>SE</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>8</td>
<td>4</td>
<td>p-cost</td>
<td>SE</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>9</td>
<td>4</td>
<td>e-cost</td>
<td>SE</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>10</td>
<td>4</td>
<td>p-cost</td>
<td>SE</td>
<td>4</td>
<td>2</td>
</tr>
</tbody>
</table>

Table 2: Experiment 1 (3 box, Stop and Execute, success based)

<table>
<thead>
<tr>
<th>Exp</th>
<th>Boxes</th>
<th>Quality</th>
<th>Control Strategy</th>
<th>Goal Orders</th>
<th>Num of Unknowns</th>
</tr>
</thead>
<tbody>
<tr>
<td>STU</td>
<td>3</td>
<td>success</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>TSU</td>
<td>3</td>
<td>success</td>
<td>CE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>TUS</td>
<td>4</td>
<td>e-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>SUT</td>
<td>4</td>
<td>p-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>UTS</td>
<td>4</td>
<td>p-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
</tbody>
</table>

Table 3: Experiment 3 (3 box, Stop and Execute, execution cost based)

<table>
<thead>
<tr>
<th>Exp</th>
<th>Boxes</th>
<th>Quality</th>
<th>Control Strategy</th>
<th>Goal Orders</th>
<th>Num of Unknowns</th>
</tr>
</thead>
<tbody>
<tr>
<td>STU</td>
<td>3</td>
<td>success</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>TSU</td>
<td>3</td>
<td>success</td>
<td>CE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>TUS</td>
<td>4</td>
<td>e-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>SUT</td>
<td>4</td>
<td>p-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
<tr>
<td>UTS</td>
<td>4</td>
<td>p-cost</td>
<td>SE</td>
<td>all</td>
<td>all</td>
</tr>
</tbody>
</table>

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Wrench Location: Each of the wrenches may initially be in any tool box. For three box experiments this implies 27 possible wrench placement scenarios.

Goal Ordering: We studied the effect of reordering the initial goals on the performance of the planner. For three box experiments, this involves 6 possible orderings.

Control Strategy: SE versus CE.

Defer/Default Decisions: The size of each bolt is either known or unknown at the start of the first planning phase. For three bolts there are 8 combinations.

Both tables, the headings along the horizontal axis indicate which of the three bolt sizes are known in the order $b_s$, $b_t$, and $b_u$ respectively. So, for instance, 4-6 indicates that bolt $b_s$ is of size 4, bolt $b_t$ is of unknown size, and bolt $b_u$ is of size 6. Vertical lines separate columns into groups with the same number of unknowns. The labels along the vertical axis denote goal orderings. For example, and ordering of TSU means the initial goal involving box T was attempted first, followed in turn by the S and U goals.

One immediate observation from Tables 2 and 3 is that more unknown information means decreased success and increased cost. Certainly the planner will be more likely to perform premature actions with less a priori information. This general trend continued throughout all of the experiments.

Major Results

In this section we will outline the major results of the experiments, and principles and heuristics we developed based on the results. The results of experiments 1 and 3 are provided in Tables 2 and 3 respectively. In each experiment, the robot begins at a neutral site (one unrelated to any work that it must do). Since the planner’s goals are strongly associated with particular tool boxes, this assumption was meant to avoid any bias in our results.

Each experiment consists of hundreds or thousands of planner runs using systematically defined sets of initial conditions, goal orderings and planning strategies. The variables defining these test sets are the following:

- **Wrench Location**: Each of the wrenches may initially be in any tool box. For three box experiments this implies 27 possible wrench placement scenarios.
- **Goal Ordering**: We studied the effect of reordering the initial goals on the performance of the planner. For three box experiments, this involves 6 possible orderings.
- **Control Strategy**: SE versus CE.
- **Defer/Default Decisions**: The size of each bolt is either known or unknown at the start of the first planning phase. For three bolts there are 8 combinations.

Table 1 provides a short summary of the ten experiments conducted. Complete experimental data can be found in [Krebsbach et al., 1991].

Choosing a Goal Ordering

One of the major results of this study was that most sensing should come as early as possible in the plan. The disadvantage of potentially premature action caused by early sensing was, in most cases, outweighed by the advantage of constructing most of the plan with more information.

Ordering Unknown Goals Early Consider Table 2, in particular, experiments STU 45- and STU 4-6. In the former, there is only one unknown, $b_u$. In the latter, there are two, $b_s$ and $b_t$, however BUMP performs at the same 63% level for both. Also, average success rates in columns with the same number of unknowns are
identical, however, the percentages in each column are distributed differently by goal ordering. For instance, in each column with one unknown there are two goal orderings which produce 100% success, and four which produce only 63% success, but the goal orderings are different in each column. Both of these behaviors are the result of a single underlying principle.

To understand this behavior, we consider an example more closely. Note that 100% success can be achieved in column 45- (of Table 2) by ordering the U-goal first (either as UST or UTS). We hypothesized that in cases where the size of $b_u$ was unknown, it was crucial to BUMP’s success to know the size of $b_u$ early in the planning process. This could be accomplished by reordering goals so that the U-goal was attacked first. If this was not done, the goal involving $b_u$ would be one of the last two BUMP would try to accomplish. Therefore, it would not sense the size of $b_u$ until later, increasing the chances that achieving it would involve undoing some actions which had already been executed. Since planning and execution are interleaved, some execution is very likely to have been performed by the time BUMP encounters its later goals. If any of the executed actions involve bolting closed a box containing a needed wrench for $b_u$, the plan will no longer be successful. Experiment 1 confirmed our suspicions that it is possible to improve average performance by controlling the goal ordering based on which information is missing for a given problem. In particular, goals involving unknown information should be considered first. The same general principle applied to Continue Elsewhere.

**Ordering to Minimize Cost** Similar observations on goal ordering can be made when cost is the quality criterion. From Table 3 we can see that the highest cost occurs when a known goal is considered first. However, looking at the -5- column, cost is minimized when there is an unknown first and an unknown last.

To better understand this behavior we conducted experiments 7 through 10 using 4 boxes (SE control strategy only). Complete results of these experiments are described in [Krebsbach et al., 1991]. These results are summarized by the following heuristic:

**Cost-Based Ordering Heuristic:** When there are goals whose achievement depends only on known information, and other goals which depend on unknowns:

1. place one unknown in the first position,
2. place one in the final position (if possible),
3. place any other unknowns following the first one,
4. place all knowns in the remaining positions.

### Choosing a Control Strategy

We found the CE strategy to be more susceptible to small increases in uncertainty, performing better than SE with one unknown, usually worse with two, and markedly worse with three. CE’s sensitivity to unknown information makes sense when one considers CE’s main advantage and disadvantage. Its advantage is that it performs more planning prior to the first execution cycle. This reduces the risk of performing premature actions if there are few unknowns, because BUMP can see further into the plan and perform action reordering to avoid conflicts it wouldn’t detect with SE until it’s too late. However, as uncertainty increases this further planning becomes less informed, and ordering decisions become more arbitrary, increasing the probability of performing premature actions which lead to failure or severe cost penalties. For instance, in the case of 3 unknowns, BUMP using CE was able to find successful plans in only 22% of the 3 box problems, as compared with 37% for SE.

### A Success-Based Overall Strategy

Let us now make a first attempt at our goal of finding a good overall planning strategy. In addition to the ordering heuristic we must have a method for selecting a control strategy and a deferral strategy. We will try to maximize success through our selection of a strategy. We will assume here that once a control strategy and a deferral strategy have been selected, the top-level goals are reordered to obtain the highest success rate for the given number of unknowns.

As we have shown, we can always improve success rates by having additional known information. Thus, if our default information were 100% reliable, it would always make sense to use it and obtain a 100% success rating (with either control strategy). Of course, default information is rarely, if ever, 100% reliable. If incorrect default information is used, the robot will most likely...
encounter an execution time error. This will necessitate some sort of execution time error recovery, and the resulting execution will certainly be inefficient. We consider this a failure. So, the increased success with extra “known” information must be adjusted by the reliability of that information. A similar point can be made regarding sensor reliability. The data in all of our experiments assume that all sensor readings are correct, and this is clearly fictional.

Analysis

To make this discussion more concrete, let us analyze the expected success rates given the reliability of our default values and our sensors. Let $r_1$, $r_2$ and $r_3$ be the reliabilities of our three defaults, $d_1$, $d_2$ and $d_3$ and let $s_1$, $s_2$ and $s_3$ be the reliabilities of the associated sensor readings. Also, assume $r_1 \geq r_2 \geq r_3$. ($d_1$, $d_2$, and $d_3$ are in no particular order relative to the planning process.) When a bolt size is known at the start of planning, this corresponds to a default reliability of 100%. Let $q_0$, $q_1$, $q_2$ and $q_3$ be the maximum potential success rates for cases with 0, 1, 2 and 3 unknowns respectively. From our experiments, these values are 1.0, 1.0, 0.67 (with CE), and 0.37 (with SE).

We can now calculate the expected success rate taking into account the default and sensor reliabilities. For example, the success rate when taking default $d_1$ and sensing the other unknowns is $r_1 s_2 s_3 q_2$. The best overall strategy in any particular instance of the three box problem can be found by computing the maximum of the following set of values:

$$\{r_1 r_2 r_3 q_0, r_1 r_2 s_3 q_1, r_1 s_2 r_3 q_1, r_1 s_2 s_3 q_1, r_1 s_2 r_3 q_2, s_1 r_2 s_3 q_2, s_1 s_2 r_3 q_2, s_1 s_2 s_3 q_3\}$$

Once the maximum is found, the associated deferral strategy consists of the default/defer decisions indicated.

It is interesting to examine the default reliabilities required in the three box domain. For simplicity, assume that all sensor readings have the same reliability $\sigma$. Table 4 shows for various values of $\sigma$ how reliable the defaults must be to make them worth taking. Looking at the column labeled $\sigma = 1.0$, we note that if the best default has reliability $\geq 0.55$ it is better to take that default than to use a 100% reliable sensor. If $r_1 \geq r_2 \geq 0.67$, it is better to take two defaults. For more realistic values of $\sigma$, we see that the defaults need not be very reliable at all. This is due to the reduction in premature actions that can be avoided by having more knowledge early in the planning process.

<table>
<thead>
<tr>
<th>Take</th>
<th>$\sigma = 1.0$</th>
<th>$\sigma = 0.8$</th>
<th>$\sigma = 0.6$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d_1$</td>
<td>$r_1 \geq 0.55$</td>
<td>$r_1 \geq 0.44$</td>
<td>$r_1 \geq .33$</td>
</tr>
<tr>
<td>$d_1, d_2$</td>
<td>$r_2 \geq 0.67$</td>
<td>$r_2 \geq 0.54$</td>
<td>$r_2 \geq .40$</td>
</tr>
<tr>
<td>$d_1, d_2, d_3$</td>
<td>—</td>
<td>$r_3 \geq 0.80$</td>
<td>$r_3 \geq .60$</td>
</tr>
</tbody>
</table>

Table 4: Success-Based Strategies.

A Cost-Based Overall Strategy

When the robot is able to detect at some point that a default value or a sensor reading was erroneous and then take corrective actions, it makes more sense to use cost as the quality criterion. As described earlier, cost can be measured either in terms of execution cost or planning effort. We will focus on execution cost since we believe this is generally the more significant aspect. A similar analysis could be developed for planning effort.

Analysis

The analysis in this case is a good deal more complicated since many more options come into play. For example, if a decision is made to try a default which later turns out incorrect, the robot could then try to recover by using a sensor. If the sensor reading also turns out to be incorrect, it might still be possible to recover with human intervention (presumably at a very high cost).\(^6\)

As before, let $r_i$ be the reliability of a default value and $s_i$ the reliability of the sensor reading. In place of the success rates $q_i$ used in our previous analysis, we need the costs under various scenarios. We define the function $C_i$ to return these costs when there are $i$ unknowns. $C_i$ takes $i$ arguments. Each argument is a sequence of one, two or three of the letters D, S and I. This sequence reflects which of the resources — default, sense and intervene — were used for the given unknown and the order in which they were tried. To ensure a cost can always be calculated, it is assumed that the last resource is successful and that intervention is always successful. For example, DS means an incorrect default followed by a correct sensor operation. SDI means an incorrect sensor reading followed by an incorrect default value followed by successful human intervention. $C_i(SDI)$ would be the cost associated with this scenario.

\(^6\)Some other options that we do not consider in this analysis are (1) to try a different sensor, and (2) to continue trying the same sensor. If the sensor is working at all (i.e., there is a non-zero probability of a correct reading), then with persistence the second option should eventually produce a correct reading. This might also have a very high cost.
Given this information we can develop formulas for the expected costs of various attempted solutions. For example, with one unknown the expected cost of defaulting with sensing and intervention as backup actions would be

\[ r_1C_1(D) + (1 - r_1)s_1C_1(DS) + (1 - r_1)(1 - s_1)C_1(DSI) \]

An alternative strategy would try sensing first followed by defaulting and then intervention.

\[ s_1C_1(S) + (1 - s_1)r_1C_1(SD) + (1 - s_1)(1 - r_1)C_1(SDI) \]

Three remaining strategies are

no default: \( s_1C_1(S) + (1 - s_1)C_1(SI) \)

no sensing: \( r_1C_1(D) + (1 - r_1)C_1(DI) \)

surrender: \( C_1(I) \)

One of these last three options might be appropriate if sensing or defaulting is particularly unreliable and the cost of intervention is light. Given the \( C_1 \) cost estimates and the reliabilities we could calculate the optimal strategy for one unknown by evaluating the five above formulas and finding the minimum.

A similar set of cost formulas can be developed for any number of unknowns (see [Krebsbach et al., 1991]), but the complexity of the formulas make them impractical. Calculating the expected cost of just one scenario that considers all three resources — default, sense and intervene — takes time \( O(n3^n) \) (with \( n \) unknowns). Even the amount of cost data that must be collected grows exponentially in the number of unknowns. Many such scenarios must be evaluated and compared to find the optimal strategy of sensing and defaulting. Clearly, we cannot effectively calculate this optimal strategy unless the number of unknowns is quite small. Rather, we need heuristic techniques that will help us find an approximately optimal strategy. This will be a goal of our future research.

Discussion

Interleaving of planning and execution has been used and discussed extensively in robotics [McDermott, 1978, Durfee and Lesser, 1986, Chapman, 1991] but few have addressed the more specific problem of deciding what to sense and when. Our work has been inspired, among others, by the work of Turney and Segre [1989], who alternate between improvising and planning. Since sensing is assumed to be expensive, the system prefers actions with the fewest sensor requests first. The results they obtained show the importance of good heuristics over sophisticated planning strategies.

Brooks [1982] verifies the feasibility of a plan in light of uncertainties and errors and decides when sensors are needed to reduce the amount of error. Doyle et al. [1986] use sensors to verify the execution of a plan. The sensor requests are generated after the plan has been produced by examining the preconditions and postconditions of each action in the plan. Domain dependent verification operators map assertions to perception requests and expectations. The entire process is done before executing the plan. Hager and Mintz [1991] have more recently proposed methods for sensor planning based on probabilistic models of uncertainty.

The need to plan with incomplete information raises important theoretical issues. A number of authors have proposed decision theoretic approaches to planning and control. Horvitz et al. [1989] propose a general model for reasoning under scarce resources that is based on decision theory. Boddy [1991] has studied time-dependent problems and proposed a framework based on decision models for constructing solutions to time-dependent problems. Chrisman and Simmons [1991] produce near optimal cost plans by using Markov Decision Processes to decide what to sense. Hsu [1990] proposes to plan with incomplete information by generating a “most general partial plan” without committing to any choice of actions not logically imposed by the information available at that point. An anytime algorithm [Dean and Boddy, 1988] is used to choose the appropriate action on the current partial plan when the system has to act.

Acknowledgement

We would like to thank Mark Boddy for useful and influential discussions about topics in this paper, most notably issues of cost analysis and decision theory.

References


